

College Algebra and College Algebra with Review Final Review

Distance Formula

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Midpoint Formula

$$\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Circles

$$(x - h)^2 + (y - k)^2 = r^2$$

Where (h, k) is the center
and r is the radius

$$\log_b(b^p) = p$$

$$b^{\log_b(p)} = p$$

$$\log_b(b) = 1$$

$$\log_b(1) = 0$$

$$\ln(x) = \log_e(x)$$

Properties of Logarithms

$$y = \log_b(x) \text{ if and only if } b^y = x$$

$$\log_b\left(\frac{M}{N}\right) = \log_b(M) - \log_b(N)$$

$$\log_b(M \cdot N) = \log_b(M) + \log_b(N)$$

$$\log_b(M^p) = p \cdot \log_b(M)$$

$$\log(x) = \log_{10}(x)$$

Change-of-Base Rule

$$\log_b(x) = \frac{\log(x)}{\log(b)}$$

$$\text{or } \log_b(x) = \frac{\ln(x)}{\ln(b)}$$

Lines

Slope

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Point-Slope Form

$$y - y_1 = m(x - x_1)$$

Slope-Intercept Form

$$y = mx + b$$

Compound Interest

Compounded n times per year

$$A = P \cdot \left(1 + \frac{r}{n}\right)^{nt}$$

A = Amount after t years

n = number of times compounded per year

r = yearly interest rate (as a decimal)

Compounded Continuously

$$A = P \cdot e^{rt}$$

P = Principal (original amount)

e = base of the natural log

t = number of years

Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Vertex of a Parabola

$$(h, k) \text{ where } h = \frac{-b}{2a} \text{ and } k = f(h)$$

Properties of Absolute Value

If $k > 0$, then $|ax + b| = k$ is equivalent to $ax + b = k$ or $ax + b = -k$.

If $k > 0$, then $|ax + b| > k$ is equivalent to $ax + b > k$ or $ax + b < -k$.

If $k > 0$, then $|ax + b| < k$ is equivalent to $-k < ax + b < k$.

The two properties above also hold for \leq and \geq

Properties of Polynomial Equations

If a polynomial $P(x)$ is divided by $x - r$, the remainder is $P(r)$.

If $P(r) = 0$, then $x - r$ is a factor of $P(x)$. If $x - r$ is a factor of $P(x)$, then $P(r) = 0$.

Even and Odd Functions

Even Function:

(y-Axis Symmetry)

$$f(-x) = f(x)$$

Odd Function:

(Origin Symmetry)

$$f(-x) = -f(x)$$