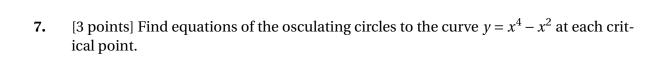
Name: M344: Calculus III (Su.19) Midterm Exam: Review Guide Chapters 13 and 14  WICHITA STATE UNIVERSITY	
	ons. Complete all problems on this paper, showing enough work. You may use any that you'd like to complete this review guide. Keep in mind that the midterm exam sed notes.
This assign	nment is optional. If submitted, it will be counted as extra credit toward your final
erwise. If	/False [1 point each] Write a <b>T</b> on the line if the statement is <u>always</u> true, and <b>F</b> oth-you determine that the statement is false, you must give justification in the space to receive credit.
1.	Let <b>r</b> be a smooth vector function. If $\ \mathbf{r}(t)\  = 1$ for all $t$ , then $\ \dot{\mathbf{r}}(t)\ $ is constant.
2.	Let <b>r</b> be a smooth vector function. If $\ \mathbf{r}(t)\  = 1$ for all $t$ , then $\dot{\mathbf{r}}(t)$ is orthogonal to $\mathbf{r}(t)$ for all $t$ .
3.	Let <b>r</b> be a vector function such that $\ddot{\mathbf{r}}(t)$ exists for all $t$ , $\dot{\mathbf{r}} \neq 0$ , and $\ddot{\mathbf{r}} \neq 0$ . Then $\mathbf{N} = \kappa \mathbf{T}$ .

\_\_\_\_\_4. Let f be a function of (x, y). If f has a local minimum at (a, b), then  $\nabla f(a, b) = \mathbf{0}$ .

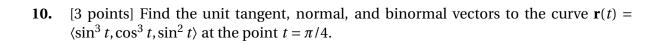
5. [1 point] Find a vector function that represents the curve of intersection of the cylinder  $x^2 + y^2 = 16$  and the paraboloid  $z = 2x^2 + 2y^2$ .

**6.** [1 point] Find the point on the curve  $y = e^{2x}$  at which the curvature is maximized.



**8.** [1 point] Reparametrize the curve  $\mathbf{r}(t) = e^t \mathbf{i} + e^t \sin t \mathbf{j} + e^t \cos t \mathbf{k}$  with respect to arclength from the point (1,0,1) in the direction of increasing t.

**9.** [1 point] Use your answer to problem **8** to compute the curvature of the space curve as a function of arclength.



11. [1 point] Consider the function  $f(x, y) = x^2 - 2x + y^2 + y$ , and let C denote the level curve f(x, y) = 5. Show that the gradient vector  $\nabla f(-1, 1)$  is orthogonal to C at the point (-1, 1).

**12.** [1 point] Let 
$$z = \sin(x + \sin t)$$
. Show that  $\frac{\partial z}{\partial x} \frac{\partial^2 z}{\partial x \partial t} = \frac{\partial z}{\partial t} \frac{\partial^2 z}{\partial x^2}$ .

13. [2 points] Find the absolute maximum and minimum values of the function  $f(x,y) = e^{-x^2-y^2}(x^2+2y^2)$  on the domain  $D: \{(x,y) \mid x^2+y^2 \le 4\}$ .

14. [1 point] Use differentials or a linear approximation to estimate the number  $(1.98)^3\sqrt{(3.01)^2+(3.97)^2}$ .

**15.** [1 point] Let  $f(x, y) = x^2 e^{-y}$ . Compute the second directional derivative  $D_{\mathbf{v}}^2 f(-2, 0)$ , where  $\mathbf{v} = \langle -3, 4 \rangle$ .